

The Bonus Divisibility Rules

Here are a bunch of additional divisibility rules that can come in handy as well. These are divided into two categories:

- *Composite Numbers*
- *Prime Numbers*

Divisibility Rules – 16 Composite Numbers

Number	Rule	Example
8	Last 3 digits form a number divisible by 8.	2520 → $520 \div 8$ ✓
9	Sum of digits divisible by 9.	2520 → $2 + 5 + 2 + 0 = 9$ ✓
12	Divisible by both 3 and 4.	2520 → $\div 3$ & $\div 4$ ✓
14	Divisible by 2 and 7.	2520 → $\div 2$ & $\div 7$ ✓
15	Divisible by 3 and 5.	2520 → $\div 3$ & $\div 5$ ✓
16	Last 4 digits divisible by 16.	2520 → $\div 16$ ✗
18	Divisible by 2 and 9.	2520 → $\div 2$ & $\div 9$ ✓
20	Last 2 digits are divisible by 20 (00, 20, 40, 60, 80).	2520 → ends in 20 ✓
21	Divisible by 3 and 7.	2520 → $\div 3$ & $\div 7$ ✓
22	Divisible by 2 and 11.	2520 → $\div 2$ & $\div 11$ ✗
24	Divisible by 3 and 8.	2520 → $\div 3$ & $\div 8$ ✓
25	Ends in 00, 25, 50, or 75.	475 → ends in 75 ✓
26	Divisible by 2 and 13.	2520 → $\div 2$ & $\div 13$ ✓
27	Sum of digits, repeated if needed, divisible by 27.	2520 → $2 + 5 + 2 + 0 = 9$ ✗
28	Divisible by 4 and 7.	2520 → $\div 4$ & $\div 7$ ✓
30	Divisible by 2, 3, and 5.	2520 → $\div 2, \div 3, \div 5$ ✓

Divisibility Rules – 6 Prime Numbers

The divisibility rule of these numbers can be generalised as follows:

$$R \pm a \times L$$

The Bonus Divisibility Rules

Where:

- R = rest of the number (excluding last digit)
- L = last digit
- a = a multiplier specific to each prime

Prime	Rule ($R \pm a \times L$)	Example
13	$R - 9L$ or $R + 4L$	$1286 \rightarrow 128 - 9 \times 6 = 74$ ✗
17	$R - 5L$	$221 \rightarrow 22 - 5 \times 1 = 17$ ✓
19	$R \pm 2L$	$1133 \rightarrow 113 + 6 = 119$ ✗
23	$R \pm 7L$	$276 \rightarrow 27 + 42 = 69$ ✓
29	$R + 3L$ or $R - 2L$	$7203 \rightarrow 720 - 6 = 714$? $714 \rightarrow 71 - 8 = 63$ ✗
31	$R - 3L$	$186 \rightarrow 18 - 18 = 0$ ✓